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Glossary

GMM Gaussian Mixture Models
HOG Histogram of Oriented Gradients
MCMC Markov Chain Monte Carlo
MSE Mean Square Error
PCA Principal Component Analysis
RGB RED GREEN BLUE
SVM Support Vector Machines

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Abstract

Object tracking – a complex challenge in the domain of computer vision – tracks a specific object such as a person, car or any other moving object in a video stream of underlying images.

Object tracking becomes useful in vehicle parking and security-based applications such as surveillance, astronomy, and so on. Once an object is locked in a given image, the object tracking model is trained with the features of that specific object, i.e. shape, color, size, presence, and position. This trained model can be used to track this specific object in a stream of images.

The complexities involved in object tracking could be due to occlusions in the images, abrupt changes in behavior of the object, i.e. speed, shape, motion of the camera, and such.

Several approaches exist today for tracking the object and in this article a new machine learning algorithm is developed which aims to achieve higher accuracies for object tracking.
A1.1 Introduction
Object tracking is one of several applications leveraging the benefits of artificial intelligence (AI). In simple terms, object tracking tracks an object of interest.

Examples include tracking a person via a video surveillance camera for security reasons, tracking an unidentified flying object in the sky, tracking a planet or a comet in night sky from the captured frames of a telescope, tracking a parked vehicle in a huge parking lot, etc.

Video captured from the cameras act as input to the object tracking system and various object tracking methods exist. Deep learning (DL) is becoming popular in object tracking-based applications; however, it requires significant processing power and may not be practical for simple or small-scale applications.

In this article, classical machine learning techniques such as PCA, HOG, SVM and Naïve Bayes are used to perform object tracking which do not require compute to the extent that deep learning does and still perform reasonably well for object tracking.

This article details two methods for object tracking – 1) HOG + PCA+ SVM  2) HOG + PCA + Naïve Bayes.

Part A of this article gives an overview of each of the feature extraction techniques such as HOG and PCA, detailing the mechanism in which these techniques extract features from a given dataset.

Part B of this article provides design and implementation of object tracking for a benchmark dataset known as dragon baby dataset. The test results were captured and a comparison of the two techniques is made based on the performance of the algorithms.

Implementation of the two techniques are done in MATLAB and the code is mentioned in the APPENDIX.

A1.2 Feature extraction techniques
Various feature extraction techniques exist of which two – PCA and HOG – are used in this article that could extract the relevant features and descriptions of the image frames in the video.

Though these two techniques are described as feature extractor’s, the actual description could be that the HOG is a feature descriptor while PCA reduces the dimensionality of the features or, in other words, maps the features to a different representation to facilitate classifier algorithm.
A1.2.1 Histogram of Gradients

A well-known approach in the field of computer vision, Histogram of Gradients (HOG) can provide feature descriptions for any given image.

A sliding window is moved over a given image and the orientation of each of the pixels is captured within the sliding window. These orientations are also called gradients and all the gradients in a sliding window form a gradient vector. These gradient vectors are used to form a histogram which reduces the matrix dimensions of the gradient vector significantly.

The magnitude of these gradients that are stored in the form of histogram are then normalized to make them robust to changes in illumination of the image. Figure 1.1 gives a glimpse of what HOG does.

![Histogram of Gradients Overview](image)

Figure 1.1: Histogram of gradients overview

A1.2.2 Principal Component Analysis

Principal component analysis (PCA) is a prominent feature reduction technique. Also known as dimensionality reduction technique.

The mathematical derivation of reducing the dimensionality can be shown by considering a dataset X which has d-dimensions.

\[ X = \{X_1, X_2, \ldots, X_d\} \]

The given dataset may or may not be centered at origin and hence its components are subtracted by the mean (\(\mu\)) of all the components.

\[ X = X - \mu \]

This can also be represented by its components as, \((X\cdot\mu) = \{(X_1\cdot\mu), (X_2\cdot\mu), \ldots, (X_d\cdot\mu)\}\)
The given dataset $X$ has to be projected onto new dimensions $e$ which in turn gives new coordinates,

\[ X' = (X-\mu)^{T}e \]

\[ X' = \begin{bmatrix} (X_1 - \mu_1)e_1 \\ (X_2 - \mu_2)e_2 \\ \vdots \\ (X_d - \mu_d)e_m \end{bmatrix} = \begin{bmatrix} (X_1 - \mu_1)e_{11} + (X_2 - \mu_2)e_{12} + \ldots + (X_d - \mu_d)e_{1d} \\ (X_1 - \mu_1)e_{21} + (X_2 - \mu_2)e_{22} + \ldots + (X_d - \mu_d)e_{2d} \\ \vdots \\ (X_1 - \mu_1)e_{m1} + (X_2 - \mu_2)e_{m2} + \ldots + (X_d - \mu_d)e_{md} \end{bmatrix} \]

The variance of the projection ($V$) = \( \frac{1}{n} \Sigma [X' - \mu]^2 \) = \( \frac{1}{n} \Sigma [\Sigma (Xe) - \mu]^2 \)

The constraints of $e$ are of unit length and hence Lagrange multiplier ($\lambda$) is introduced,

\[ V = \frac{1}{n} \Sigma [\Sigma (Xe)]^2 \] - \lambda [(\Sigma e)^2 - 1]

The eigen vectors are in the direction of maximum variance and hence it's essential to find the maximum.

\[ \frac{\partial V}{\partial e} = \frac{2}{n} \Sigma (\Sigma xe)x - 2\lambda e = 0 \]

\[ \Sigma e = \lambda e \] where $\lambda$ is the eigen value

Figure 1.2: PCA dimensionality reduction
Principal components are nothing but the eigen vectors in the new dimension e. Hence for a given dataset \( X \), the principal components can be found by first projecting the vectors to a new dimension and then finding the eigen vectors of the new dimensional data. The number of eigen vectors is equal to the number of principal components as shown in Figure 1.2.

A1.3 Classification techniques
Several classification techniques exist of which two of the techniques – SVM and Naïve Bayes – are used in this article that could classify the features extracted from the video frames.

SVM is generally more suitable in combination with HOG feature descriptor but in this article, we will also use Naïve Bayes as a classification technique to compare the outcomes.

A1.3.1 Naïve Bayes
Naïve Bayes is one of the oldest classification techniques that uses Bayes theorem from probability theory for performing classification.

According to Bayes theorem, \( P(A/B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B/A) \cdot P(A)}{P(B)} \); where \( P(B) = \sum P(B/A) \cdot P(A) \)

The Bayes theorem represents, Posterior = \( \frac{\text{Likelihood} \cdot \text{Prior}}{\text{Evidence}} \)

If we consider \( \omega_1 \) and \( \omega_2 \) are two classes and \( x \) is a dependent vector then as per Bayes theorem,

\[
P(\omega_i/x) = \frac{P(x/\omega_i) \cdot P(\omega_i)}{P(x)} ; \text{ where } P(x) = \sum P(x/\omega_i) \cdot P(\omega_i) \text{ and } \omega_i \text{ can be } \omega_1 \text{ or } \omega_2.
\]

For a given \( x \), if \( P(\omega_1/x) > P(\omega_2/x) \); then class \( \omega_1 \) is decided else class \( \omega_2 \) is decided. This case of 2 class classification can be easily extended to multiple classes.

A1.3.2 Support Vector Machine
Support vector machines (SVM) is a classifier that is non-probabilistic in nature and the classification happens through a hyperplane. The simplest form of SVM is a linear SVM whose hyperplane is linear and the other could be the nonlinear SVM which uses a kernel trick to perform the classification.

Let’s consider a 2-class SVM classifier where the aim is to separate the data using a higher dimensional hyperplane \( (\omega \cdot x + b = 0) \).
To separate the data, one would intend to maximize the separation as much as possible, which is dependent on the nearest data point from either side of the class to the hyperplane and those nearest points in either side can be represented using $(\omega \cdot x^+ + b = +1)$ and $(\omega \cdot x^- + b = -1)$ as shown in Figure 1.3.

$$\omega \cdot x^+ + b = +1$$
$$-\omega \cdot x^- + b = -1$$

The difference between these nearest points represented hyperplanes gives the margin and the goal is to maximize this margin. Since $\omega$ is a vector, it is divided both sides with $|\omega|$ to obtain the margin length.

$$\frac{\omega}{|\omega|} \cdot (x^+ - x^-) = \frac{2}{|\omega|}$$

Maximizing the margin length $\frac{2}{|\omega|}$ is same as minimizing $\frac{1}{2} * |\omega|^2$ and thus we introduce Lagrange multiplier ($\alpha>0$) to solve the constraint optimization problem.

Lagrange function, $L(\omega, b, \alpha) = \frac{1}{2} * |\omega|^2 - \sum \alpha \cdot [y(\omega \cdot x + b) - 1]$
Minimizing the Lagrange function \[ \frac{\partial L}{\partial b} = \Sigma \alpha.y = 0 \] and \[ \frac{\partial L}{\partial \omega} = \Sigma \alpha.y.x = 0 \]

\[ y = f(x) = \Sigma \alpha.y.x^T.x + b \], which is the decision boundary or the hyperplane that classifies the data.

The term \( x^T.x \) indicates the dot product and means that it’s a projection of one vector over another which means it is computing similarity of the data points:

1) If \( x^T.x \) are perpendicular, then dot product is 0.
2) If \( x^T.x \) are in same direction, it implies large +ve value indicating that they are on +ve side of the hyperplane.
3) If \( x^T.x \) are in same direction, it implies large -ve value indicating that they are on -ve side of the hyperplane.

This classification is based on the linearly separable data else one needs to use kernel trick to classify the data which is a nonlinear SVM.

**B2.1 Loading the video and division into frames**

The video frame dataset called dragon baby dataset was taken with 20 video frames of which 10 video frames are used as training dataset and 10 of the video frames are used as testing dataset.

Figure 2.1 shows the steps to load the video frames into the MATLAB program and details the reading of ground truth data for those 10 video frames for training.

The ground truth data is loaded into a cell array and mapped to each video frame that is read which highlights the object of interest in each frame.
Figure 2.1: Loading the video frames

Figure 2.2 shows the 10-video frame dragon baby dataset for training where the head of the baby is the object of interest and all other parts of the image are background.

Figure 2.2: Loading the dragon baby dataset training images
B2.2 Implementation of feature extraction - HOG

The MATLAB implementation of histogram of oriented gradients technique is mentioned in APPENDIX 1 and 2.

The training dataset consisting of 10-video frames is considered along with its corresponding ground truth that highlights the baby's head or in other words, the object of interest and any other part of the frame is considered as background.

Each video frame image is cropped in according to the ground truth so that the features of the object of interest can be extracted using histogram of oriented gradients technique. Similarly, the features of background of the image is also extracted and labelled appropriately.

Figure 2.3 shows the cropped video frame images of the training dataset based on the given ground truth data. The head of the baby is the object of interest or, in other words called as foreground.

Figure 2.3: Training dataset video frames cropped as per ground truth
Figure 2.4 details the non-objects of the video frame images considered as background of the images and are labelled accordingly.

These background features help classifier during training in differentiating the features of foreground (object) vs. the background so that the classifier can easily predict the foreground or object from the testing images.

**B2.3 Implementation of feature reduction - PCA**

The extracted features of the foreground and background of the video frame images using histogram of oriented gradients are then passed through principle component analysis so that the dimensionality of the features is reduced by selecting appropriate principle components that has the most variance in the feature data.

![Figure 2.4: Background of the video frames of training dataset](image)

The MATLAB code for PCA is mentioned in Appendix 1 and 2.
The feature vectors extracted for both foreground and background objects using histogram of gradients are reshaped appropriately so that can be processed using principle component analysis.

During feature reduction using principle component analysis, the 2 principle components are extracted and are labelled as foreground (1) and background (0) as per whether the principle components are retrieved from foreground feature vector or background feature vector.

Similar mechanism is also used during testing phase except that instead of 2 principle components, a single principle component is used to classify the image by classifier.

**B2.4 Implementation of classification techniques SVM and Naïve Bayes**

In this section, the classification techniques such as support vector machines and Naïve Bayes are used as classification techniques to track the object.

As discussed in sections B2.2 and B2.3, the features of the foreground and background objects of the video frame image dataset are extracted using histogram of oriented gradients and then the dimensionality of the features is reduced through principle component analysis. These labelled reduced feature set of foreground and background objects is used to train the support vector machine model.
The trained SVM model is used to test the reduced feature set resulted from the histogram of oriented gradients and the principle component analysis. Figure 2.5 details the flowchart of the algorithm that is used to track objects using support vector machines. The support vector machine gets modelled and a decisive boundary is formed based on trained features and the formed decision boundary classifies the testing dataset features into foreground and background.
The 2\textsuperscript{nd} technique used as a classifier is the Naïve Bayes classifier which replaces the support vector machine mentioned earlier. The labelled reduced feature set of foreground and background objects of training dataset are used to train the Naïve Bayes model.

The trained Naïve Bayes model is used to test the reduced feature set resulting from the histogram of oriented gradients and the principle component analysis. Figure 2.6 details the flowchart of the algorithm that is used to track objects using Naïve Bayes classifier. The Naïve Bayes gets modelled and the posterior probabilities of each class (foreground and background) are formed based on trained features and the formed posterior probabilities classifies the testing dataset features into foreground and background.

Figure 2.6: Flowchart detailing the object tracking algorithm using Naïve Bayes
The MATLAB code of SVM classification technique is mentioned in APPENDIX 1 and the MATLAB code of Naïve Bayes classification technique is mentioned in APPENDIX 2.

**B2.5 Measure to evaluate Object tracking**

The object tracking is performed on a given set of testing video frame images as shown in Figure 2.7. The object detection is performed as pattern recognition task by extracting the features of the testing images using HOG and PCA and then passing the extracted features to the trained Naïve Bayes / SVM classifier.

In this section, the objective is to perform object detection and analyze which classification technique – support vector machines or Naïve Bayes classifier – performs better.

![Figure 2.7: Testing video frame dataset consisting of 10-frames](image)
Figure 2.8: Object (Baby head) tracking using SVM classification
Figure 2.9: Object (Baby head) tracking using Naïve Bayes classification

Figure 2.8 is the output of the object tracking algorithm with classification technique support vector machines and Figure 2.9 is the output of the object tracking algorithm with classification technique Naïve Bayes.

During testing phase the input video frame image was scanned through a window of fixed size for matching the feature similarities with object trained and the image window having the maximum similarity is the object of interest. The similarity metric used in this algorithm is cosine similarity which is computed as inner product of two vectors divided by their corresponding product of norms.

\[
\text{Cosine Similarity of vectors } A \text{ and } B = \frac{A \cdot B}{\text{norm}(A) \times \text{norm}(B)}
\]

Where vector A corresponds to the fixed size moving window patch on the image and vector B corresponds to the object feature vector used during training.
B2.6 Performance evaluation of the Classifiers

Figure 2.10 details the performance evaluation of both algorithms on a frame-by-frame basis.

![Performance evaluation of Object Tracking](image)

Figure 2.10: Performance evaluation of object tracking

It can be observed from Figure 2.10 that both algorithms (SVM and Naïve Bayes) perform almost similar while their mean time execution varies greatly, as per Table 2.1.

<table>
<thead>
<tr>
<th>Technique</th>
<th>Mean time taken (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SVM Classification for object tracking</td>
<td>1125.5</td>
</tr>
<tr>
<td>Naïve Bayes classification for object tracking</td>
<td>3082.9</td>
</tr>
</tbody>
</table>

Table 2.1: Mean time of execution of the two object tracking algorithms

Based on Figure 2.10 and Table 2.1, it can be concluded that SVM classification technique performs better than Naïve Bayes classification technique for object tracking of dragon baby dataset.
References


Appendix

Appendix 1 – MATLAB code for object tracking using HOG, PCA and SVM

clc;

clear;

close all;

tic;

sf = dir('C:\Users\dell\Documents\DragonBaby\DragonBaby\img\*.jpg');

nl=length(sf);

fileID = fopen('C:\Users\dell\Documents\DragonBaby\DragonBaby\drag_gt.txt');

gt = textscan(fileID,'%f %f %f %f','Delimiter',' ,');

fclose(fileID);

vf=[];

v1=[];

v2=[];

for u = 1:10

filename = strcat('C:\Users\dell\Documents\DragonBaby\DragonBaby\img\',sf(u).name);

im= double(rgb2gray(imread(filename)));

x1=gt{1,1}(u);

y1=gt{1,2}(u);

w1=gt{1,3}(u);

h1=gt{1,4}(u);

face = imcrop(im,[x1,y1,w1,h1]);

[featureVector1,hogVisualization] = extractHOGFeatures(face);

bkgrd = imcrop(im,[160,140,w1,h1]);

[featureVector2,hogVisualization] = extractHOGFeatures(bkgrd);
[r,c]=size(featureVector1);
%v1=[v1;featureVector1];
%v2=[v2;featureVector2];
fv1=reshape(featureVector1,[8,c/8]);
fv2=reshape(featureVector2,[8,c/8]);

[Train_coeff1] = pca(fv1);
[Train_coeff2] = pca(fv2);

v1=[v1,Train_coeff1(:,1:2)];
v2=[v2,Train_coeff2(:,1:2)];

vf=horzcat(v1,v2);
trainf=vf';

figure(1);
subplot (3,4,u);
imshow(uint8(im));

figure(2);
subplot (3,4,u);
imshow(uint8(face));

figure(3);
subplot (3,4,u);
imshow(uint8(bkgrd));

end
```matlab
k = 1;
for i1 = 11:20
    filename = strcat('C:\Users\dell\Documents\DragonBaby\DragonBaby\img', sf(i1).name);
    im1 = double(rgb2gray(imread(filename)));
    [m n] = size(im1);
    fv = 0;
    csf = 0;
    for i = 20:m-h1
        for j = 100:n-(6*w1)
            it = im1(i:i+h1, j:j+w1);
            [featureVector3, hogVisualization] = extractHOGFeatures(it);
            fv = fv + 1;
            fv3 = reshape(featureVector3, [8, c/8]);
            [Test_coeff3] = pca(fv3);
            tc = Test_coeff3(:, 1:1);
            tc = tc';
            ans = predict(SVMModel, tc);
            if ans == 1
                cs = (featureVector3*featureVector1')/(norm(featureVector3)*norm(featureVector1))';
                if cs > csf
                    csf = cs;
                    xf = j;
                    yf = i;
                end
            end
```
end
end
end

imf=imcrop(im1,[xf,yf,w1,h1]);

figure(4);
subplot(3,4,k);
imshow(uint8(im1));

figure(5);
subplot(3,4,k);
imshow(uint8(imf));

similarity(k)=csf;
k=k+1;
end

figure(6);
plot(1:10,similarity,'-b*');
xlabel('Image Names');
ylabel('Cosine Similarity with object (Face)');
title('Performance evaluation of Object tracking');
ti=toc
Appendix 2– MATLAB code for object tracking using HOG, PCA and Naïve Bayes

clc;
clear;
close all;

tic;
sf = dir('C:\Users\dell\Documents\DragonBaby\DragonBaby\img\*.jpg');
nl=length(sf);

fileID = fopen('C:\Users\dell\Documents\DragonBaby\DragonBaby\drag_gt.txt');
gt = textscan(fileID,'%f %f %f %f','Delimiter','\n');
cfclose(fileID);

vf=[];
v1=[];
v2=[];
for u = 1:10
    filename = strcat('C:\Users\dell\Documents\DragonBaby\DragonBaby\img\',sf(u).name);
    im= double(rgb2gray(imread(filename)));
    x1=gt{1,1}(u);
y1=gt{1,2}(u);
w1=gt{1,3}(u);
h1=gt{1,4}(u);
    face = imcrop(im,[x1,y1,w1,h1]);
    [featureVector1,hogVisualization] = extractHOGFeatures(face);

    bkgrd = imcrop(im,[160,140,w1,h1]);
    [featureVector2,hogVisualization] = extractHOGFeatures(bkgrd);
[r,c]=size(featureVector1);

%v1=[v1;featureVector1];
%v2=[v2;featureVector2];
fv1=reshape(featureVector1, [18, c/18]);
fv2=reshape(featureVector2, [18, c/18]);

[Train_coeff1] = pca(fv1);
[Train_coeff2] = pca(fv2);

v1=[v1,Train_coeff1(:,1:2)];
v2=[v2,Train_coeff2(:,1:2)];

vf=horzcat(v1,v2);
trainf=vf';

figure(1);
subplot (3,4,u);
imshow(uint8(im));

figure(2);
subplot (3,4,u);
imshow(uint8(face));

figure(3);
subplot (3,4,u);
imshow(uint8(bkgrd));
end

k=1;
for i1 = 11:20

filename = strcat('C:\Users\dell\Documents\DragonBaby\DragonBaby\img\',sf(i1).name);

im1= double(rgb2gray(imread(filename)));  
[m n]=size(im1);
fv=0;
csf=0;
for i=20:m-h1
  for j=100:n-(6*w1)
    it=im1(i:i+h1,j:j+w1);
    [featureVector3,hogVisualization] = extractHOGFeatures(it);
    fv=fv+1;
    fv3=reshape(featureVector3,[18,c/18]);
    [Test_coeff3] = pca(fv3);
    tc=Test_coeff3(:,1:1);
    tc=tc';
    ans = predict(NB_Model,tc);
    if ans==1
      cs=((featureVector3*featureVector1')/(norm(featureVector3)*norm(featureVector1)))';
      if cs > csf
        csf=cs;
      end
    end
  end
end
xf=j;
yf=i;
end
end
end

imf=imcrop(im1,[xf,yf,w1,h1]);

figure(4);
subplot(3,4,k);
imshow(uint8(im1));

figure(5);
subplot(3,4,k);
imshow(uint8(imf));

similarity(k)=csf;
k=k+1;
end

figure(6);
plot(1:10,similarity,'--b*');
xlabel ('Image Names');
ylabel ('Cosine Similarity with object (Face)');
title('Performance evaluation of Object tracking');
ti=toc
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